COS	226	Fall	2011	HWO2
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200 + 50★ pts.; 4 pages.

Due 2011-10-04 2:05 p.m.

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Please refer to the previous assignment for important instructions on the allowable use of resources and the requirements for electronic and hardcopy submission. Use the newsgroup for questions, clarifications, and general discussion related to this homework and class. Ensure that everything you submit is neat and easy to comprehend; otherwise, it will be ignored, with zero credit. You are encouraged to answer the three \star questions for extra credit but do note that those questions are graded much more strictly than the others.

- 1. (1 pt.) Write your name in the space provided above.
- 2. (1 pt.) The pen-and-paper questions in this assignment need to be answered on separate sheets of paper that must be neatly attached to your hardcopy submission with a single staple. Note the number of additional pages attached here:
- 3. (1 pt.) Package and submit your solutions to the programming questions via http://cs.umaine.edu/~chaw/u/. After submitting your work, fill in the following:

File name:	
Size, in bytes:	
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4. (17 pts.) A k-tree, for k > 1, either is empty or consists of a node r, called its root, and a sequence of $c \le k$ subtrees, each of which is a nonempty k-tree. The roots of these c subtrees are the *children* of r, and r is their *parent*.

Depict all distinct (i.e., nonisomorphic) 4-trees with n nodes, for n = 0, 1, 2, 3, 4, 5.

- 5. (10 pts.) A labeled k-tree is a k-tree in which each node with c > 1 children is associated with a sequence of labels $l_1, l_2, \ldots, l_{c-1}$.
 - Indicate the number of distinct labeled 4-trees with n nodes, for n = 0, 1, 2, 3, 4, 5, with labels drawn from the domain $\{1, 2, 3\}$. A tree need not contain all the labels from the domain, and labels may be repeated. You do not need to depict the trees, but you must explain clearly how you arrive at the answers. There is no credit for answers without proper explanations.
- 6. (20 pts.) A k-search-tree is a labeled k-tree with the following additional constraints on each node n with c > 1 children, where we define $l_0 = -\infty$ and $l_c = \infty$ for convenience.
 - The labels are strictly increasing; that is, $l_i < l_{i+1}$ for $i = 0, 2, \dots c 1$.
 - If x_1, x_2, \ldots, x_c are the children of n, then all labels in the subtree rooted at the x_i t are greater than the label l_{i-1} and less than the label l_i , for $i = 1, 2, \ldots, c$.

Depict all distinct labeled 4-search-trees with n nodes, for n = 0, 1, 2, 3, 4, 5, with labels drawn from the domain $\{1, 2, 3, 4, 5\}$.

- 7. (10 pts.) Depict a k-search-tree in which some label l occurs in two distinct locations, or explain clearly why no such tree exists.
- 8. (30 pts.) Describe efficient algorithms for the following, given k-search-tree tree. For each algorithm, provide (1) a clear English description, (2) detailed pseudocode, and (3) a proof that the algorithm's running time is O(h) where h is the height of the k-search-tree.
 - (a) Locating a given label in the tree or determining that it is absent from the tree.
 - (b) Inserting a given label into the tree or determining that it is already in the tree.
 - (c) Removing a given label from the tree or determining that the tree does not contain that label.
- 9. (10 pts.) Conduct an experimental evaluation of the three algorithms for the maximum contiguous subsequence sum problem described in the textbook.¹ Ensure that your results are meaningful, given the limited clock accuracy and other factors. In your electronic submission, include a plain text ASCII file that tabulates the running times for input sequences of varying lengths. Describe in that file how the input sequences are generated, and why that generation process is suitable. (Example: Do not exclusively use sequences that contain only positive or only negative numbers.) Explain any discrepancies between your results and those predicted by the textbook. Also include in your submission a portable PDF [sic] file that depicts the running time data in a suitable graphical form.

Note the file names here:	
text results and explanation:	
graphical results:	

10. (90 pts.) Implement your algorithms of Question 8 as part of the simple record-manager application described below. Package and submit your source code as in the previous assignment, being sure to include adequate documentation. Poorly written or poorly documented code is likely to receive zero credit.

The record manager stores key-data pairs of the form (k,d) where k is a non-negative integer and d is floating point number. (You may assume that k and d fit in Java's int and float types.) All user interaction with the record manager is through a text-mode command language based on the standard-input/standard-output interface. The input consists of one command per line. The record manager reads and responds to each command in turn. Except for the xp command, the response to each command is also a single newline-terminated line. The syntax and semantics of the commands, and the desired outputs, are as follows. We use the symbol \sqcup to denote a single space character.

 $^{^1{\}rm Mark}$ Allen Weiss, Data Structures and Problem Solving Using Java, 4th edition (Addison-Wesley, 2010), §5.3.

command	actions			
c⊔k	Create a record manager that contains no records and			
	that uses a k-search-tree with the given value of k. The			
	output is an empty line (single newline character).			
s⊔k⊔d	The pair (k,d) is stored in the record manager. If a			
	pair of the form (k, d') already exists, then the new pair			
	replaces it. The output is an empty line.			
e⊔k	If the record manager contains the key k then the output			
	is 1 else the output is 0.			
$r \sqcup k$	The data d associated with key k is retrieved from the			
	record manager. The output is d . If the key k is absent			
	from the record store, the output consists of an empty			
	line.			
$d_{\sqcup}k$	If there is a record with key k then it is deleted. The			
	output is an empty line.			
XS	The output is the size of the tree (a single integer).			
xh	The output is the height of the tree.			
xa	The output is a list of the key-data pairs in the tree, in			
	preorder. All pairs are printed on a single line, with a			
	single space separating adjacent pairs. Each pair (k, d)			
	is printed using the parenthesized format $(k \ d)$, where			
	there is a single space separating k and d .			
xb	The output is similar to that of xa but the nodes are to			
	be listed in postorder.			
xp	The output consists of the following two-dimensional text			
	representation of the current state of the tree used to			
	store the records. This representation of a tree t contains			
	one line for each node of t. The line representing a node			
	$n \in t$ consists of n's (k,d) pair, printed as in the xa			
	command, prefixed with 3d spaces, where d is the depth			
	of n in t . Further, all the lines representing descendants			
	of a node precede the line representing that node's right			
	sibling, if any.			

Ensure that (1) your program produces exactly the output described above, with no spurious text such as extra spaces or newlines, prompts, or other messages and (2) your program reads from standard input and writes to standard output, with no additional assumptions on either.

11.	(10 pts.)	Conduct	t an experime	ental evalua	ation of e	each comr	nand of yo	ur record	-manager
	implemen	ntation,	following the	guidelines	of Ques	tion 9.			

- 12. (20 pts.) \star Describe an efficient algorithm for generating all k-search-trees with n nodes, with labels drawn from L, where k, n, and L are provided as input. Provide an English description and pseudocode. Explain why the algorithm is correct. Determine and prove its running time. Implement the algorithm and conduct an experimental study of the running time. Package and submit your implementation as in earlier questions.
- 13. (20 pts.) \star Describe modifications to the algorithms of Question 8 that ensure that the height of a k-search-tree with n nodes is $O(\log n)$. Follow the instructions of Question 12.
- 14. (10 pts.) ★ Provide an efficient algorithm for pretty-printing a k-search-tree based on conventional graphical notation using ASCII graphics. Use the newsgroup for elaboration of this question and document and package your results as in Question 12.