

1. Write your name below.
  
2. Trace the execution of the FIND-MAX-CROSSING-SUBARRAY algorithm on the array **A** depicted below, with the arguments **low**, **mid**, and **high** equal to 1, 5, and 10, respectively.

|       |    |    |   |     |    |     |     |     |    |     |
|-------|----|----|---|-----|----|-----|-----|-----|----|-----|
| i:    | 1  | 2  | 3 | 4   | 5  | 6   | 7   | 8   | 9  | 10  |
| A[i]: | 88 | 19 | 9 | -66 | -2 | 116 | -56 | -12 | 87 | 101 |

List the values of *sum* and *left-sum* after each iteration of the first for-loop of the algorithm. Similarly, list the values of *sum* and *right-sum* after each iteration of the second for-loop.

3. Depict the recursion tree that outlines the recursive calls made by the FIND-MAXIMUM-SUBARRAY algorithm when invoked on the array of Question 2 (repeated below), with `low` and `high` equal to 1 and 10, respectively. The nodes of the tree should be labeled with the function invoked (FIND-MAXIMUM-SUBARRAY or FIND-MAX-CROSSING-SUBARRAY and the edges should connect each function's node to the node of its invoker.

|       |    |    |   |     |    |     |     |     |    |     |
|-------|----|----|---|-----|----|-----|-----|-----|----|-----|
| i:    | 1  | 2  | 3 | 4   | 5  | 6   | 7   | 8   | 9  | 10  |
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4. Demonstrate the *recursion tree* method on the recurrence  $T(n) = 4T(n/3) + 5n$ .

5. Demonstrate the application of the substitution method with guess  $T(n) = cn^{\log_3 4}$  to the recurrence of Question 4. Explain where the proof breaks down.

6. Modify the guess of Question 5 to allow the use of the substitution method to prove that  $T(n) = O(n^c)$ , for a suitable constant  $c$ .

7. Prove the result of Question 6 using the *master method*.